Table 1Truth table.				
x	у	z	$x + \overline{x}y + \overline{xy}z$	x + y + z
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	1	1
1	0	0	1	1
1	0	1	1	1
1	1	0	1	1
1	1	1	1	1

1.

- **a.** CAPEX stands for Capital expenses, i.e. costs associated with the acquirement or upgrade of physical assets such as equipment, property or industrial buildings.
- **b.** OPEX stands for Operating expenses, i.e., the ongoing costs for performing the production.

2.

- a. A KPI is a measure of performance. Each KPI is a single number.
- b. Downtime: Describes how large part of the time that a system has not been producing. Can indicate if there are reliability issues.Yield: Describes how much product is obtained per raw material. Used to indicate how much waste there is in the production.
- **3.** \overline{x} can be removed from the second term since that term can only affect the value of the expression when x is false, otherwise the expression is always true. For the same reason, \overline{xy} can now be removed from the third term which yields the right hand side.

Alternatively this can be shown with a truth table, see Table 1.

4.

a. The constraints can be formulated as

 $1x_1 + 2x_2 <= 22$ $12x_1 + 4x_2 <= 96$ $5x_1 + 5x_2 <= 60$

where x_1 and x_2 is the production rate of Super and Nova respectively. With the additional constraints $x_1 \ge 0$ and $x_2 \ge 0$, the area of admissible solutions is given in Figure. 1. As can be seen, there are 5 vertexes where the optimal solution can be located. The five are given by

$$\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 2 & 6 & 8 \\ 0 & 11 & 10 & 6 & 0 \end{bmatrix}$$

Given the prices $p_1 = 7$ and $p_2 = 4$, the revenue for the company in each vertex is

$$\begin{bmatrix} p_1 \\ p_2 \end{bmatrix}^T \begin{bmatrix} 0 & 0 & 2 & 6 & 8 \\ 0 & 11 & 10 & 6 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 44 & 54 & 66 & 56 \end{bmatrix}$$

The optimal production rate is consequently $x_1 = 6$ and $x_2 = 6$ and the revenue is 66.



Figure 1 Admissible solutions

- **b.** The intersection of the capacity limits of forming and bristling machine is at $x_1 = 5.2$ and $x_2 = 8.4$. This corresponds to a capacity usage of 68 in the packaging machine and it is consequently the minimum capacity level that can achieve this.
- **c.** If the price p_1 is lowered, production will move from $x_1 = 6$ and $x_2 = 6$ to $x_1 = 2$ and $x_2 = 10$. The break-point can be formulated as

$$6p_1 + 24 = 2p_1 + 40$$
$$p_1 = 4$$

Hence, at 4, the company moves away from the original product mix. The revenue at that point is 48.

5.

- a. Batch, the ICs are produced in batches.
- **b.** The solution is shown in Figure 2.

6.

a. See lecture slides.

b. The area utility matrix becomes

$$Au = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}.$$

$\ensuremath{\mathbf{c}}\xspace$. The utility operation matrix is

$$U = \begin{bmatrix} 1 & 1 & 1 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 & 0 & 1 & 0 & 1 \end{bmatrix}$$

d. The direct loss J_p is calculated as

$$Jp = (1 - A_{av}^{Dir}) \cdot * q_m \cdot * p * n_s$$



Figure 2 Solution to Problem 5

and becomes

$$Jp = [9 \quad 120 \quad 24 \quad 0 \quad 60]^T$$
.

7.

a. The plant structure is drawn in Figure 3.



Figure 3

The current factory has a single-path structure. As the new factories have interconnected parallel processing and parallel ovens, they will have a network structure.

b. It is a master recipy.

General and site recipies do not have any information about the production equipment. A control recipies is a single execution instances of a master recipy.

8.

a. Optimization of the quadratic profit functions gives

$$egin{array}{rcl} B_1(Q_2) &=& \max(0,2-c_1-Q_2)/2 \ B_2(Q_1) &=& \max(0,2-c_2-Q_1)/2. \end{array}$$

b. We need to find solutions to the simultaneous equations

$$egin{array}{rcl} Q_1^* &=& \max(0,2-c_1-Q_2^*)/2 \ Q_2^* &=& \max(0,2-c_2-Q_1^*)/2. \end{array}$$

If we first assume that $Q_1^* = 0$ then the 2nd equation gives $Q_2^* = 1 - c_2/2$. Inserting this again in the 1st equation gives the condition $2 - c_1 - (1 - c_2/2) \le 0$ which is equivalent to $2 - 2c_1 + c_2 \le 0$. This describes the area in the (c_1, c_2) plane where $(Q_1^*, Q_2^*) = (0, 1 - c_2/2)$ holds, i.e. a monopoly situation for firm 2.

By symmetry we have $(Q_1^*, Q_2^*) = (1 - c_1/2, 0)$, i.e. monopoly for firm 1, in the area where $2 - 2c_2 + c_1 \leq 0$.

When both Q_1^{\ast} and Q_2^{\ast} are positive we have the equation system

$$egin{array}{rcl} Q_1^* &=& (2-c_1-Q_2^*)/2 \ Q_2^* &=& (2-c_2-Q_1^*)/2. \end{array}$$

which has the solution $(Q_1^*, Q_2^*) = \left(\frac{2-2c_1+c_2}{3}, \frac{2-2c_2+c_1}{3}\right).$

With a sufficiently large difference in manufacturing costs the duopoly market hence collapses into a monopoly.

