



• A portfolio optimization problem $x_{3}(t) \text{ and } x_{4}(t) \text{ quantifies increased capacity:} \\ Sawing: 7x_{1} + 10x_{2} \le 100 + x_{3}(t) \\ Assembling: 16x_{1} + 12x_{2} \le 135 + x_{4}(t) \\ \hline \\ Mini \text{ problem} \\ \hline \\ Mini \text{ problem} \\ \hline \\ Mini \text{ problem} - \text{ solution} \\ \hline \\ Sawing capacity attime t = 3: \\ x_{3}(3) = 0.7x_{3}(2) + 30u_{3}(2) = 0.7(0.7x_{3}(1) + 30u_{3}(1)) + 30u_{4}(2) \\ = 0.7(0.7x_{3}(0) + 30u_{4}(2)) + 30u_{4}(2) \\ = 0.7(0.7(0.7x_{3}(0) + 30u_{4}(1)) + 30u_{4}(2) \\ = (0.7^{2} + 0.7 + 1)30 = 65.7 \\ \hline \\ Stationary capacity atter three weeks, i.e. x_{3}(3)? \\ \hline \\ What is the stationary sawing capacity of the extra labor? \\ \hline \\ What is the stationary sawing capacity of the extra labor? \\ \hline \\ \\ \hline \\ Dynamic Production planning example cont'd \\ The weekly cost for extra personnel is p_{3} and p_{4} respectively This gives the following production planning problem that optimizes one year aftead production: \\ max p_{1}(1x_{1}(1) + 2x_{2}(1) + 30u_{3}(1) - p_{4}(1)u_{4}(t) \\ subject to x_{3}(t) + 10.7x_{3}(t) + 40.5w_{4}(t) \\ Tx_{1}(t) + 10.5w_{1}(t) + 20.7x_{3}(t) + 40.5w_{4}(t) \\ Tx_{1}(t) + 10.5w_{2}(t) \leq 105 + x_{4}(t) \\ 0 \leq u_{5}(t) \leq 10 - x_{4}(t) \leq 10 \\ x_{3}(0) = x_{3}^{2} - x_{4}(0) = x_{4}^{2} \\ \text{for } t = 0, \dots Scal + x_{4}(t) \leq 105 + x_{4}(t) \\ 0 \leq u_{5}(t) \leq 10 - x_{4}(t) \leq 10 \\ x_{3}(0) = x_{3}^{2} - x_{4}(0) = x_{4}^{2} \\ \text{for } t = 0, \dots Scal + x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} and x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} and x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} and x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} and x_{4}^{2} are the initial capacities for the extra personel x_{4}^{2} and x_{4}^{2} are the initial capacities for the extra personel x_{$	Today's lecture	Dynamic Production planning example
• LP is production planning example • Static systems • Subject systems • Model Predictive Control • A portfolio optimization problem • Mini problem Assume that extra sawing personel is working full-time, i.e. $u_3(t) = 1, t = 0, 1,$ • Mini problem • Mini problem • Mini problem • Solution Sawing capacity at time $t = 3t$: $x_3(3) = 0.7x_3(2) + 30u_3(2) = -0.7(x_3(1) + 30u_3(1)) + 30u_3(2)$ $= (0.7^2 + 0.7 + 1)30 = 65.7$ Stationary capacity at time $t = 3t$: $x_3(3) = 0.7x_3(2) + 30u_3(2) = -0.7(x_3(1) + 30u_3(1)) + 30u_3(2)$ $= (0.7^2 + 0.7 + 1)30 = 65.7$ Stationary capacity is given by: $x_3 = 0.7x_3 = 30$ which gives $x_3 = \frac{30}{0.7} = \frac{30}{0.3} = 100$ The total sawing capacity is doubled after learning period Dynamic Production planning example contl Optimal production planning problem that optimizes one year aftered production: max $p_1(x_1(t) + p_{0.7}(t_2)(t) - p_{0.0}(u_3(t)) - p_{0.0}(u_4(t)))$ $u_3(t) + 120x_3(t) \leq 13 + x_{31}(t)$ $u_3(t) + u_3(t) + 10 - x_{31}(t) + 30u_{32}(t) \leq 1$ $u_3(t) + u_3(t) + 10 - x_{31}(t) = 10$ $u_3(t) + u_3(t) + u_3(t) + 10 - x_{31}(t) + 10 - x_{31$		Hire extra personel to increase production:
DefinitionState in the state of the state in	 Linear Programming (LP) 	Nominal learning (sawing):
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