

Steam

- Cooling water
- Electricity
- Fuel
- Water treatment
- Combustion of tail gas
- Nitrogen
- Water



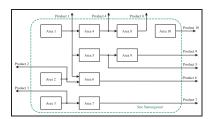


Vacuum system

# Why disturbances in utilities?

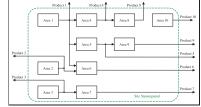
Disturbances in utilities

- affect many areas at a site, directly or indirectly
- are common within the process industry



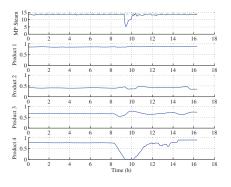
Also, root cause hard to determine because of utility interdependence.

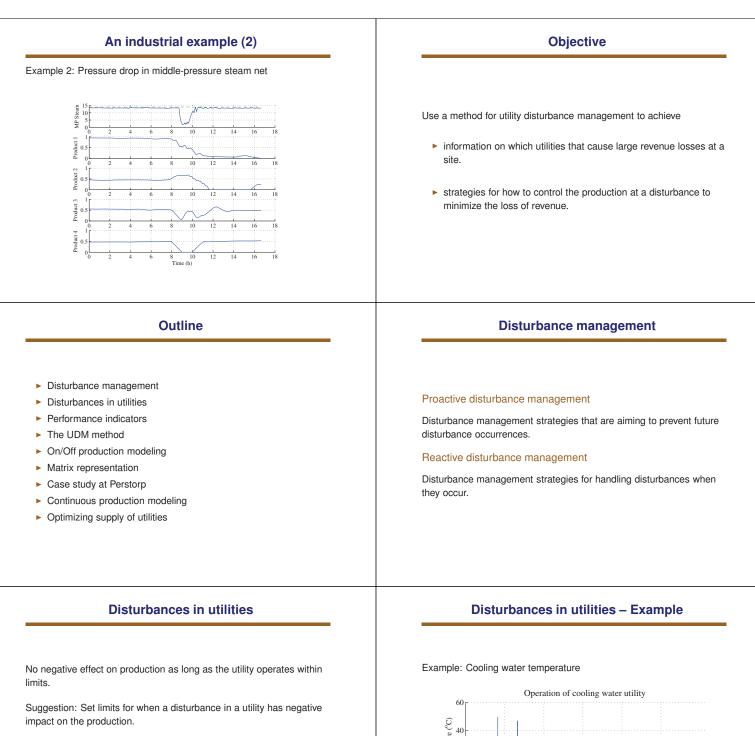




### An industrial example (1)

Example 1: Pressure drop in middle-pressure steam net





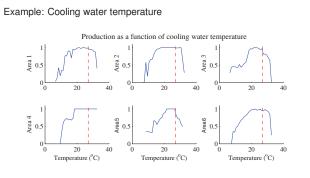
lempera

01–Aug-07 29–Jan–08 29–Jul–08 27–Jan–09 28–Jul–09 26–Jan–10

- ► Steam: Steam pressure outside certain limits
- Cooling water: Cooling water temperature outside certain limits
- ► ...

 $\Rightarrow$  Utility disturbances can be identified from measurement data.

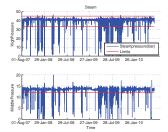
### Validation of limits



### Availability computations

#### Example: Steam

Disturbance limits, pressure p: High pressure steam: p< 33 bar or p> 45 bar Middle pressure steam: p< 12 bar



Steam availability = 95.94 %

# Area availability

#### Definition

The *direct area availability* is the fraction of time all utility parameters for all utilities needed at an area are inside their critical limits.

### **Utility availability**

#### Definition

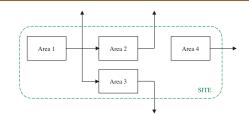
*Utility availability* is the fraction of time all utility parameters are inside their critical limits.

# Utilities required at each area

Each area at a site requires a specific set of utilities.

	Area 1	Area 2	Area 3	Area 4
Steam	х	х		
Cooling water	х	х	х	х
Electricity	х	х	х	х
Fuel	х			
Water treatment utility		х		х
Combustion of tail gas	х	х		
Nitrogen	х	х	х	х
Water	х	х	х	х
Compressed air	х	х	х	х
Vacuum system	х	х	х	

### Area interdependence

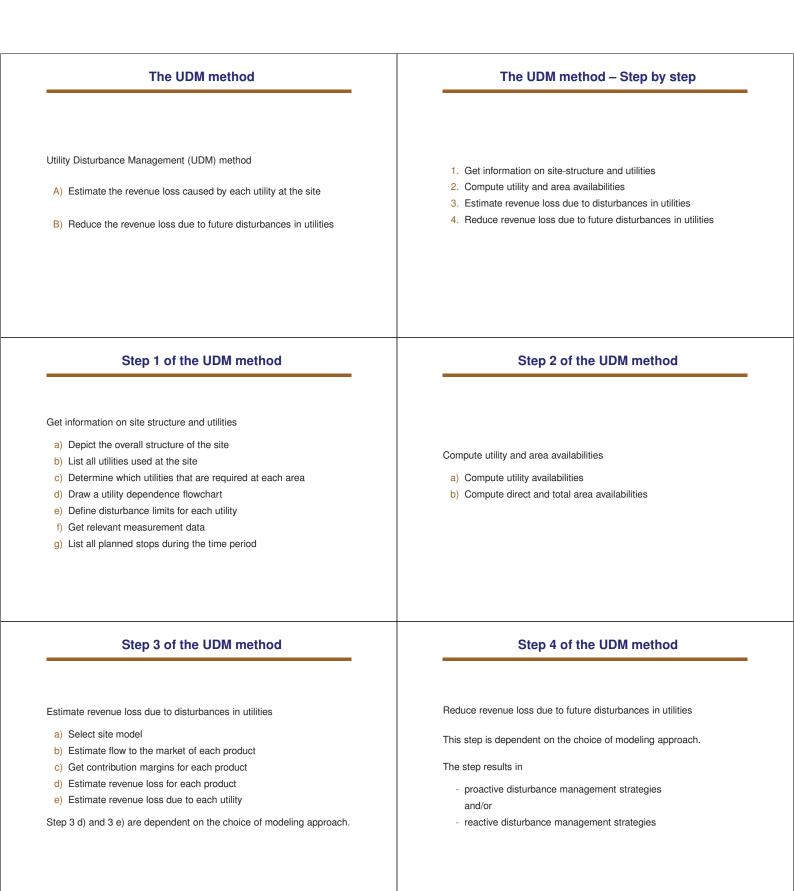


#### Definition

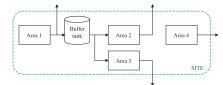
The *total area availability* is the fraction of time all utility parameters for all utilities needed at an area are inside their critical limits

AND

all areas which the area is dependent on are available.



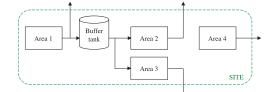
# **On/off production modeling**



- Utilities and areas are considered to be either operating or not operating, i.e. 'on' or 'off'.
- An area operates at maximum production speed when available, and does not operate when not available.
- Including or not including buffer tanks between areas.

#### Matrix representation

#### Representation of the interconnection of production areas



Area dependence matrix

$$A_d = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

(size  $n_a \times n_a$ )

#### Matrix representation

Utility operation matrix

U =	1	1	0	0	1	1	1	1	0	1 -
	1	1	1	1	0	0	1	1	1	1
U =	1	1	1	1	1	1	0	1	1	1
	1	0	0	1	1	1	1	1	1	1
	1	1	1	1	1	1	1	0	0	1

(size  $n_u \times n_s$ )

### UDM: On/off without buffer tanks

Use utility and area availabilities to estimate revenue loss

- + Simple modeling; Only need to know which utilities that are required by each area and how areas are connected
- + Orders utilities according to the revenue loss they cause
- + Worst case estimates of revenue losses
- Greatly overestimates the revenue losses
- Only information about WHICH utilities that cause large losses, no information on HOW to improve the availabilities of these utilities
- Internal buffer tanks not included  $\Rightarrow$  No decision support for choosing buffer tank levels
- No dynamics included  $\Rightarrow$  No reactive disturbance management strategies may be obtained

#### **Matrix representation**

Representation of utility measurement data

steam =	[42]	38	34	32	35	41	40	36	34	37]
cooling water =	[25]	24	24	26	28	30	27	25	24	25]
electricity =	[1	1	1	1	1	1	0	1	1	1]
feed water $=$	[22]	19	18	20	22	21	21	21	21	21]
instrument air $=$	[1	2	1	1	3	2	1	0	0	1]

#### Disturbance limits:

Steam :	pressure < 35 bar
Cooling water :	temperature $> 27^{\circ}C$
Electricity :	on/off
Feed water :	pressure < 20 bar
$Instrument \ air:$	pressure $\leq 0$ bar

#### **Matrix representation**

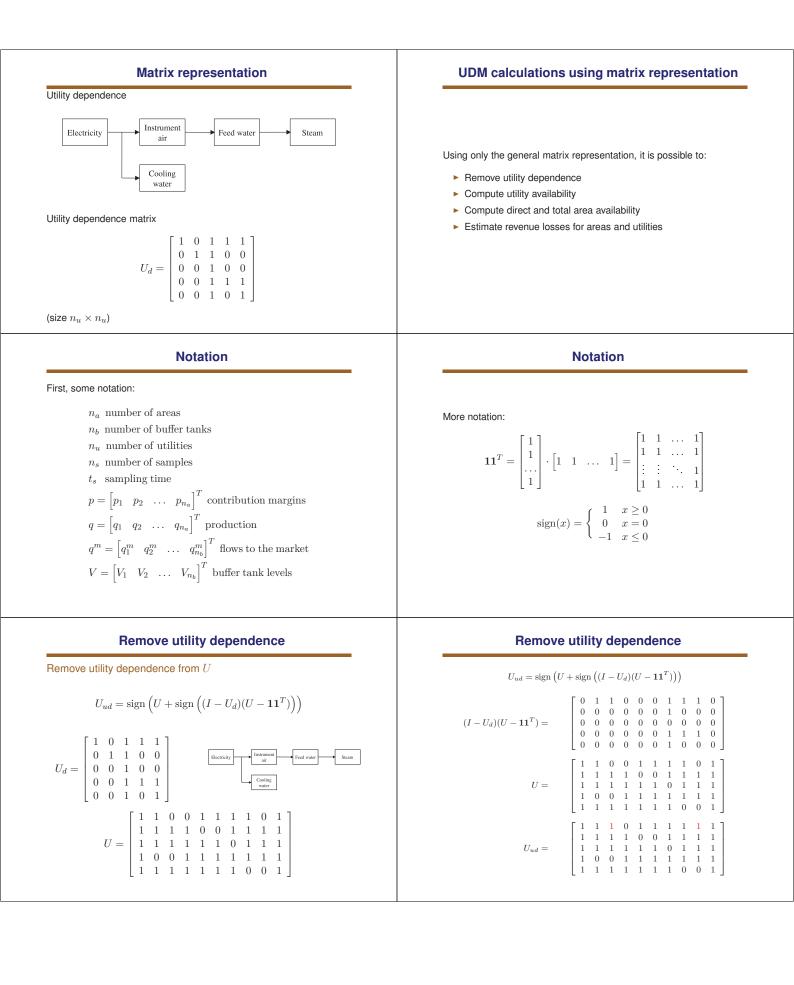
Utility requirements

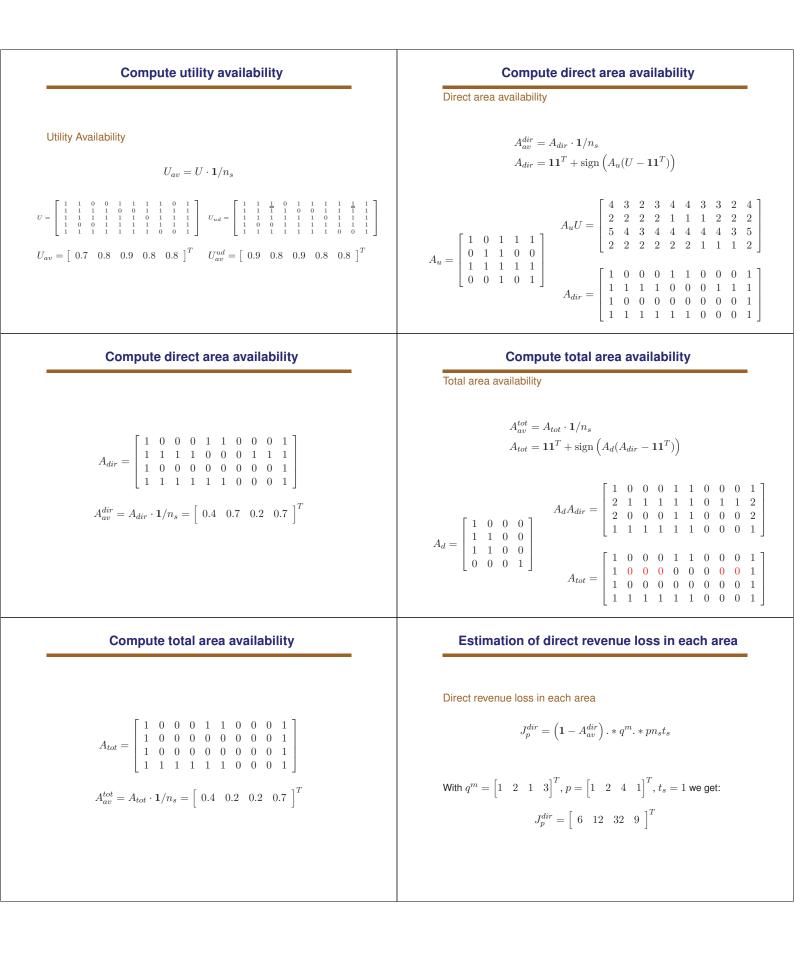
	Area 1	Area 2	Area 3	Area 4
Steam	х		х	
Cooling water		х	х	
Electricity	х	х	х	х
Feed water	х		х	
Instrument air	х		х	х

Area-utility matrix

$$\mathbf{A}_u = \begin{bmatrix} 1 & 0 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 \end{bmatrix}$$

(size  $n_a \times n_u$ )





# Estimation of total revenue loss in each area

Total revenue loss in each area

$$J_p^{tot} = \left(\mathbf{1} - A_{av}^{tot}\right) \cdot * q^m \cdot * pn_s t_s$$

With 
$$q^m = \begin{bmatrix} 1 & 2 & 1 & 3 \end{bmatrix}^T$$
,  $p = \begin{bmatrix} 1 & 2 & 4 & 1 \end{bmatrix}^T$ ,  $t_s = 1$  we get:  
$$J_p^{tot} = \begin{bmatrix} 6 & 32 & 32 & 9 \end{bmatrix}^T$$

### Estimation of total revenue loss due to each utility

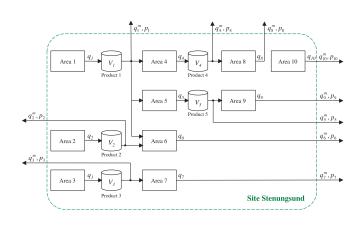
Total revenue loss due to utilities

$$J_{u}^{tot} = \operatorname{diag}\left[\mathbf{1} - U_{av}^{ud}\right] \cdot \operatorname{sign}\left(A_{d}A_{u}\right)^{T} (q^{m} \cdot \ast p) n_{s} t_{s}$$

$$\operatorname{diag} \begin{bmatrix} \mathbf{1} - U_{av}^{ud} \end{bmatrix} \cdot \operatorname{sign} (A_d A_u)^T = \begin{bmatrix} 0.1 & 0.1 & 0.1 & 0 \\ 0 & 0.2 & 0.2 & 0 \\ 0.1 & 0.1 & 0.1 & 0.1 \\ 0.2 & 0.2 & 0.2 & 0 \\ 0.2 & 0.2 & 0.2 & 0.2 \end{bmatrix}$$

With 
$$q^m = \begin{bmatrix} 1 & 2 & 1 & 3 \end{bmatrix}^T$$
,  $p = \begin{bmatrix} 1 & 2 & 4 & 1 \end{bmatrix}^T$ ,  $t_s = 1$ :  
 $J_u^{tot} = \begin{bmatrix} 9 & 16 & 12 & 18 & 24 \end{bmatrix}^T$ 

# Flowchart of the product flow



### Estimation of direct revenue loss due to each utility

Direct revenue loss due to utilities

$$\begin{split} J_u^{dir} &= \mathrm{diag} \begin{bmatrix} \mathbf{1} - U_{av}^{ud} \end{bmatrix} \cdot A_u^T (q^m \cdot *p) n_s t_s \\ &\mathrm{diag} \begin{bmatrix} \mathbf{1} - U_{av}^{ud} \end{bmatrix} \cdot A_u^T = \begin{bmatrix} 0.1 & 0 & 0.1 & 0 \\ 0 & 0.2 & 0.2 & 0 \\ 0.1 & 0.1 & 0.1 & 0.1 \\ 0.2 & 0 & 0.2 & 0 \\ 0.2 & 0 & 0.2 & 0.2 \end{bmatrix} \\ &\mathrm{With} \; q^m = \begin{bmatrix} 1 & 2 & 1 & 3 \end{bmatrix}^T, \; p = \begin{bmatrix} 1 & 2 & 4 & 1 \end{bmatrix}^T, \; t_s = 1; \\ & J_u^{dir} = \begin{bmatrix} 5 & 16 & 12 & 10 & 16 \end{bmatrix}^T \end{split}$$

### **Case study at Perstorp**

- UDM method applied to site Stenungsund, Perstorp
- On/off production modeling without buffer tanks



**Site Stenungsund** Located on the Swedish west coast, 50 km north of Gothenburg.

Main products: Aldehydes, organic acids, alcohols, plasticizers

WINNING FORMULAS

### **Utility requirements**

	1	2	3	4	5	6	7	8	9	10
Steam HP							х	х	х	х
Steam MP	х	х	Х	х	х	х	х		х	
Cooling water	х	х	х	х	х	х	х	х	х	х
Cooling fan 1	х									
Cooling fan 2		х								
Cooling fan 3			Х							
Cooling fan 7							х			
Electricity	х	х	Х	х	х	х	х	х	х	х
Water treatment	х	х	Х	х	х	х		х	х	
Flare	х	х	Х	х	х	х				х
Combustion device 7							х			
Combustion device 9									х	
Nitrogen	х	х	Х	х	х	х	х	х	х	х
Feed water	х	Х	Х	х	х			х		
Instrument air	х	х	х	х	х	х	х	х	х	Х

### Summary of case study problem

- 10 production areas
- ▶ 15 utilities
- ► 5 internal buffer tanks
- August 1, 2007 July 1, 2010
- Planned stop September 15 October 8, 2009
- Sampling interval 1 minute
- $\Rightarrow$  Size  $15\times1~501~921$  of the utility operation matrix

### **Case study matrices**

	$A_{i}$	$_d =$		0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		0 (0 0 (1 0 1 0 (0 0 (1 0 (1 0 (1 0 (1) 0 (0 0 (0) 0 (0	) () ) () 1 () ) 1 ) () () () () () 1 () ) 1	) (() ) () ) () ) () ) () ) ()	) (() ) (() ) (() ) () ) () ) (()	) () ) () ) () ) () ) () ) 1)	) () ) () ) () ) () ) () ) () ) () ) ()	) () ) () ) () ) () ) () ) () ) () 1 ()				
$A_u =$	$\begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix}$	$     \begin{array}{c}       1 \\       1 \\       1 \\       1 \\       1 \\       1 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       1 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\       0 \\      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#### Estimates of revenue losses caused by each utility

Direct loss	Total loss
Cooling water	Cooling water
MP steam	MP steam
Combustion device 9	Cooling fan 1
Combustion device 7	Feed water
Cooling fan 1	Combustion device 9
Electricity	Combustion device 7
HP steam	Electricity
Feed water	HP steam
Nitrogen	Cooling fan 2
Cooling fan 3	Cooling fan 3
Cooling fan 2	Nitrogen
Instrument air	Instrument air
Cooling fan 7	Cooling fan 7
Flare	Flare
Water treatment	Water treatment

### **Continuous production modeling**

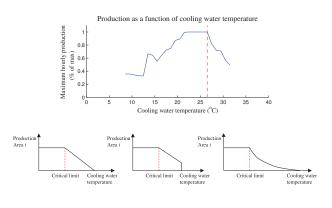
#### **Case study conclusions**

- The cooling water utility seems to cause the greatest losses at site Stenungsund
- Proactive disturbance management:
   Improve availability of cooling water utility

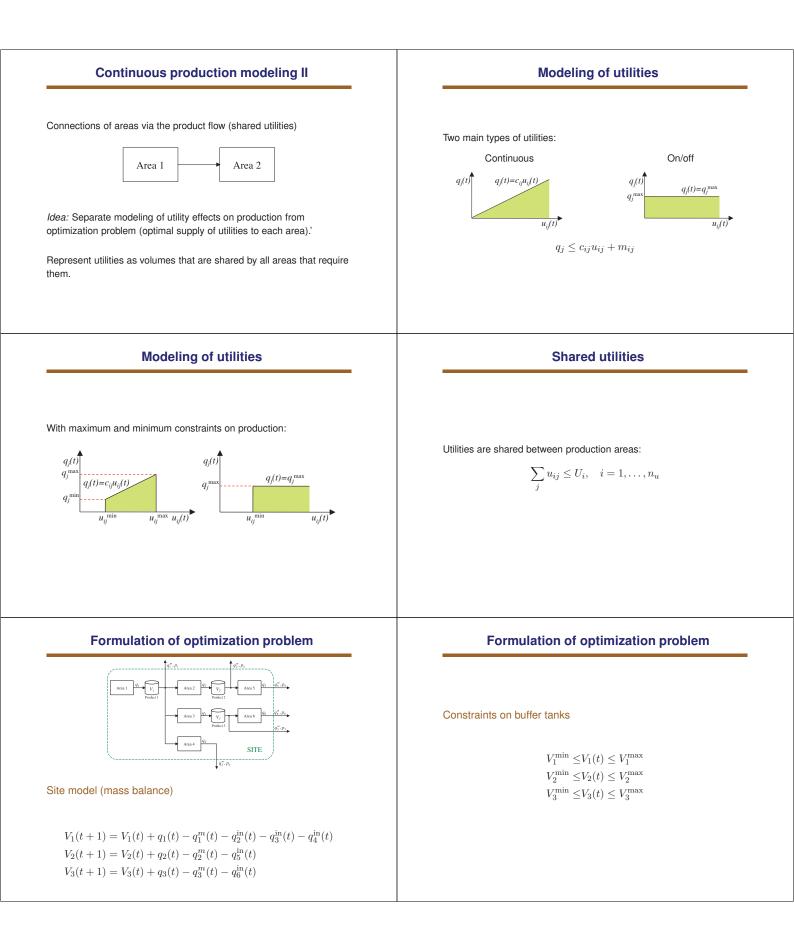
Remaining question: How should disturbances in the supply of utilities be handled, when they occur?

# Continuous production modeling I

Effects of disturbances in utilities on production



- Effects of disturbances in utilities on production
- Shared utilities (+connections of areas via the product flow)



# Formulation of optimization problem

Constraints on production rates

$$q_i^{\min} \le q_i(t) \le q_i^{\max}$$

or

Constraints on production rates

$$q_i^{\min} + s_i(t) \le q_i(t) \le q_i^{\max}$$
$$-q_i^{\min} \le s_i(t) \le 0$$

if shutdown/start-up of areas should be penalized.

### Formulation of optimization problem

$\text{Area} \rightarrow$	1	2	3	4	5	6
Steam HP	х		х			
Steam MP		х		х		Х
Cooling water	х	Х	Х	х	Х	Х

Constraints due to shared utilities

$$\frac{1}{c_{11}}q_1(t) + \frac{1}{c_{13}}q_3(t) \le U_1(t)$$
$$\frac{1}{c_{22}}q_2(t) + \frac{1}{c_{24}}q_4(t) + \frac{1}{c_{26}}q_6(t) \le U_2(t)$$
$$\sum_{i=1}^6 \frac{1}{c_{3i}}q_i(t) \le U_3(t)$$

### Formulation of optimization problem

#### Dynamic optimization

Minimize deviation from optimal steady-state operation. Cost function (e.g.):

$$J_t = (p^T q^m(t) - p_{ref})^2 Q_p + \Delta V^T(t) Q \Delta V(t) + \Delta q^T(t) R \Delta q(t)$$

where

$$\Delta V(t) = V(t) - V_{ref}$$
$$\Delta q(t) = q(t) - q_{ref}$$

Add terms  $-g^T s(t) + s^T(t) Q_s s(t)$  if shutdown of areas should be penalized.

#### Formulation of optimization problem

due to shared utilities 
$$\sum_{j\in\mathcal{M}_i}u_{ij}(t)\leq U_i(t),\quad i=1,\ldots,n_u$$
 
$$q_j(t)\leq c_{ij}u_{ij}(t)+m_{ij}$$

Continuous

Constraints

$$\sum_{j \in \mathcal{M}_i} \frac{1}{c_{ij}} q_j(t) - \frac{m_{ij}}{c_{ij}} \le U_i(t)$$

On/off

$$q_j(t) \leq \begin{cases} q_j^{\max} & \text{if } U_i(t) = 1 \\ 0 & \text{if } U_i(t) = 0, \end{cases} \quad j \in \mathcal{M}_i$$

### Formulation of optimization problem

#### Steady-state optimization

Optimal steady-state operation determined from linear program:

maximize 
$$\sum_{q,q^m}^{n_a} p^T q^m$$
  
subject to constraints

 $\Rightarrow$  Optimal profit  $p_{ref},$  optimal production rates  $q_{ref},$  optimal flows to market  $q_{ref}^m$  in steady state.

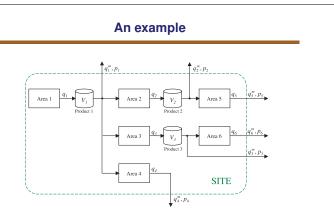
### Formulation of optimization problem

Dynamic optimization

minimize 
$$\sum_{\tau=0}^{N-1} J_t\left(q(\tau), q^m(\tau), V(\tau), s(\tau)\right)$$

subject to constraints

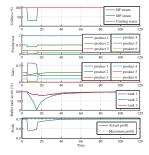
For online disturbance management, the optimization problem may be solved in receding horizon fashion (MPC).

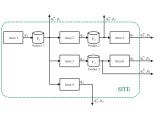


Assume utilities are shared equally at maximum production. How should utility resources be divided when a disturbance in a utility occurs?

# Solution to dynamic optimization problem

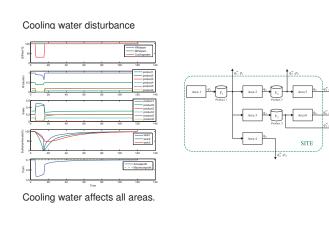
#### MP steam disturbance

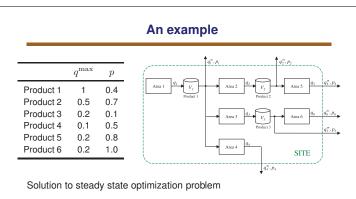




MP steam affects area 2, 4 and 6.

### Solution to dynamic optimization problem



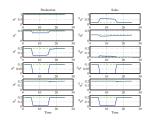


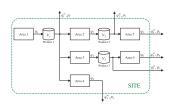
 $q_{\text{ref}} = \begin{bmatrix} 1 & 0.5 & 0.2 & 0.1 & 0.2 & 0.2 \end{bmatrix}^{T}$  $q_{\text{ref}}^{m} = \begin{bmatrix} 0.2 & 0.3 & 0 & 0.1 & 0.2 & 0.2 \end{bmatrix}^{T}$ 

with the optimal profit  $p_{\rm ref} = 0.7$ .

# Solution to dynamic optimization problem

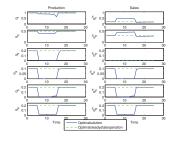
#### MP steam disturbance

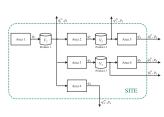




### Solution to dynamic optimization problem

#### Cooling water disturbance





#### UDM: Continuous production modeling

Continuous representation of utilities and areas.

- + Find and evaluate reactive disturbance management strategies
- + Process understanding by simulations
- + MPC as a tool for online disturbance management
- Much modeling effort needed
- Could be hard to identify utilities effect on production

### **Documentation**

- A General Method for Handling Disturbances on Utilities in the Process Industry, Anna Lundholm, Hampus Carlsson, Charlotta Johnsson, 18th IFAC World Congress, Milamo, Italy, 2011 (the general idea, motivation)
- A Tool for Utility Disturbance Management, Anna Lundholm, Charlotta Johnsson, 14th IFAC Symposium on Information Control Problems in Manufacturing, Bucharest, Romania, May 2012 (the on/off model case)
- Formulating an Optimization Problem for Minimization of Losses due to Utilities, Anna Lindholm, Pontus Giselsson, International Symposium on Advanced Control of Chemical Processes, Singapore, July 2012. (the continuous model case)

# Summary

- Disturbances in utilities cause great losses at industrial sites.
- Their effect is hard to predict since they are shared between production areas, that are connected by the product flow.
- The UDM method is a general method for utility disturbance management.
- The UDM method with on/off production modeling is a tool for quickly ordering the utilities at a site according to the loss they cause. The computations can be carried out efficiently using a matrix representation.
- The UDM method with continuous production modeling gives both proactive and reactive disturbance management strategies. MPC may be used for online disturbance management.