FRTN15 Predictive Control—Home Work 1 Signals and Systems

In this homework exercise we recapitulate theory for discrete time signals and systems in assignments 1-3. Recursive Least square estimation (RLS) is treated in assignment 4. The exercise also gives the opportunity to practice Matlab/Simulink.

E-mail your detailed and motivated solutions in pdf-format to fredrikb@control.lth.se. Attach any Matlab code or Simulink models you might have used.

1. Sample the (continuous time) system

$$G_{y,u}(s) = \frac{s+1}{s^2}.$$

Provide the transfer function and a state space representation. Conduct the calculations

- **a.** by hand, with a parametrized sample period h.
- **b.** using matlab, with sample period h = 0.1.
- **c.** How does the sampling period affect the result?
- **2.** Give the transfer function H(z) from r to y of the interconnection below, where $H_1(z) = z + 2$, $H_2(z) = \frac{1}{z^2 + 2z + 1}$ and $H_3(z) = \frac{z}{z+2}$. Also plot the response y when r is a step function.



3.

a. Show that the system H given by

$$x(kh+h) = \begin{pmatrix} 1 & h \\ 0 & 1 \end{pmatrix} x + \begin{pmatrix} \frac{h^2}{2} \\ h \end{pmatrix} u(kh)$$
$$y(kh) = \begin{pmatrix} 1 & 0 \end{pmatrix} x(kh)$$

is not asymptotically stable. Here h > 0 denotes the sampling period.

- **b.** Stabilize H by means of linear state feedback. The resulting system should have all eigenvalues placed in the origin; use h = 0.1. (Hint: The command **acker** in the matlab control system toolbox can be useful.)
- c. Placing all eigenvalues in the origin is referred to as deadbeat control. Give an interpretation, motivating this nomenclature. What potential drawbacks are there, compared to less aggressive eigenvalue placements? Hint: Study how the feedback gain changes when h approaches zero.

- **4.**
 - **a.** Use Simulink to demonstrate RLS identification of $\Theta = [a \ b]^T$ for $y_k = ay_{k-1} + bu_{k-1} + w_k$, where w_k is a normal white noise process. *Hint:* If you use Simulink, the the block 'Matlab function' might be useful. Also type 'help persistent. at the Matlab prompt.
 - **b.** Comment on the choice of input signal and how it affects the result.
 - c. Assume a is time varying, how can the method be modified to identify a? How do you use information about typical speed of change of a to tune the algorithm?