



****/l_12 :- 0--

Model Predictive ControlMinimize a cost function,
$$V$$
, of inputs and predicted outputs. $V = V(U, Y_1)$, $U_2 = \begin{bmatrix} w(t + N - 1) \\ w(t) \end{bmatrix}$, $Y_1 = \begin{bmatrix} y(t + A/E) \\ y(t + D/Q) \end{bmatrix}$, $Y_1 = \begin{bmatrix} y(t + A/E) \\ y(t + D/Q) \end{bmatrix}$. V often quadratic $V(U, Y_2) = Y_1^TQ_2Y_2 + U_2^TQ_2U_1$ $W(U, Y_2) = Y_1^TQ_2Y_2 + U_2^TQ_2U_1$ $W(t, Y_2) = Y_2^TQ_2Y_2 + U_2^TQ_2U_1$ $w(t) = -L2(t/t)$ $W(t, Y_2) = Y_2^TQ_2Y_2 + U_2^TQ_2U_1$ $W(t) = Cx(t + K_1)$ $W(t) = Cx(t + K_1)$

$$A = \begin{pmatrix} 1 & 0.139 \\ 0 & 0.861 \end{pmatrix}, \quad B = \begin{pmatrix} 0.214 \\ 2.786 \end{pmatrix}, \quad C = \begin{pmatrix} 1 & 0 \end{pmatrix}$$

Minimize $V(U_t) = ||Y_t - R||$ where $R = \begin{pmatrix} r \\ \vdots \\ r \end{pmatrix}, r$ =reference,
 $M = 8, N = 2, u(t+2) = u(t+3) = u(t+7) = \dots = 0$

$$Y_t = \begin{pmatrix} CA^8 \\ \vdots \\ CA \end{pmatrix} x(t) + \begin{pmatrix} CA^6B & CA^7B \\ \vdots & \vdots \\ 0 & CB \end{pmatrix} \begin{pmatrix} u(t+1) \\ u(t) \end{pmatrix}$$
$$= D_x x(t) + D_u U_t$$

Solution without control constraints

$$U_t = -(D_u^T D_u)^{-1} D_u^T D_x x + (D_u^T D_u)^{-1} D_u^T R = = -\begin{pmatrix} -2.50 & -0.18\\ 2.77 & 0.51 \end{pmatrix} \begin{pmatrix} x_1(t) - r\\ x_2(t) \end{pmatrix}$$

Use

$$u(t) = -2.77(x_1(t) - r) - 0.51x_2(t)$$







	A library of analysis objects
iqc_gui('fricSYSTEM')	
<pre>extracting information from fricSYSTEM scalar inputs: 5 states: 10 simple q-forms: 7 LMI #1 size = 1 states: 0 LMI #2 size = 1 states: 0 LMI #3 size = 1 states: 0 LMI #4 size = 1 states: 0 LMI #5 size = 1 states: 0 Solving with 62 decision variables ans = 4.7139</pre>	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
The friction example in text format	Summary
<pre>d=signal; % disturbance signal e=signal; % error signal w1=signal; % friction force w2=signal; % delay perturbation u=signal; % delay perturbation u=signal; % control force v=tf(1,[1 0])*(u-w1) % velocity x=tf(1,[1 0])*v; % position e==d-x-w2; u==10*tf([2 2 1],[0.01 1 0.01])*e; w1==iqc_monotonic(v,0,[1 5],10) w2==iqc_cdelay(x,.01) iqc_gain_tbx(d,e)</pre>	 Gain scheduling Internal model control Model predictive control Nonlinear observers Lie brackets Extra: Integral quadratic constraints
Next: Lecture 14	
Course Summary	