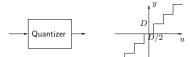
Lecture 8 — Backlash and Quantization

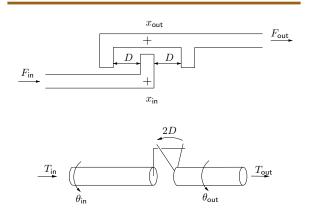
Today's Goal:

► To know models and compensation methods for backlash

Be able to analyze the effect of quantization errors



Linear and Angular Backlash



Backlash

Backlash (glapp) is

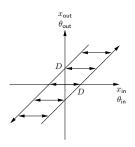
- present in most mechanical and hydraulic systems
- increasing with wear
- bad for control performance
- may cause oscillations

Note: A gear box without any backlash will not work if temperature rises

The Standard Model

Assume instead

- $\dot{x}_{out} = \dot{x}_{in}$ when "in contact"
- $\dot{x}_{out} = 0$ when "no contact"
- No model of forces or torques needed/used



Material

Lecture slides

Note: We are using analysis methods from previous lectures (describing functions, small gain theorem etc.), and these have references to the course book(s).

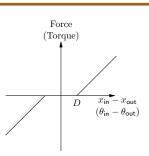
Example: Parallel Kinematic Robot

Gantry-Tau robot: Need backlash-free gearboxes for high precision



EU-project: SMErobotTM www.smerobot.org

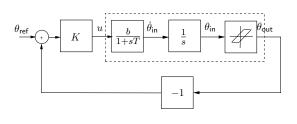
Dead-zone Model



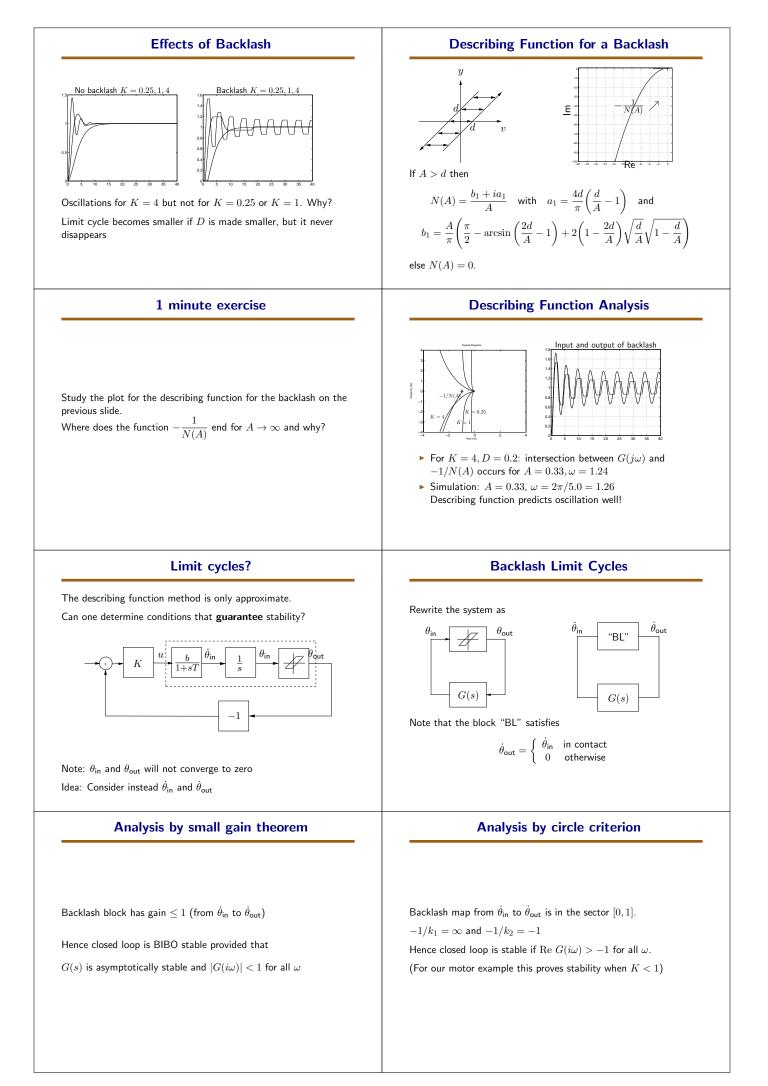
- Often easier to use model of the form $x_{in}(\cdot) \rightarrow x_{out}(\cdot)$
- ▶ Uses implicit assumption: $F_{out} = F_{in}, T_{out} = T_{in}$. Can be wrong, especially when "no contact".

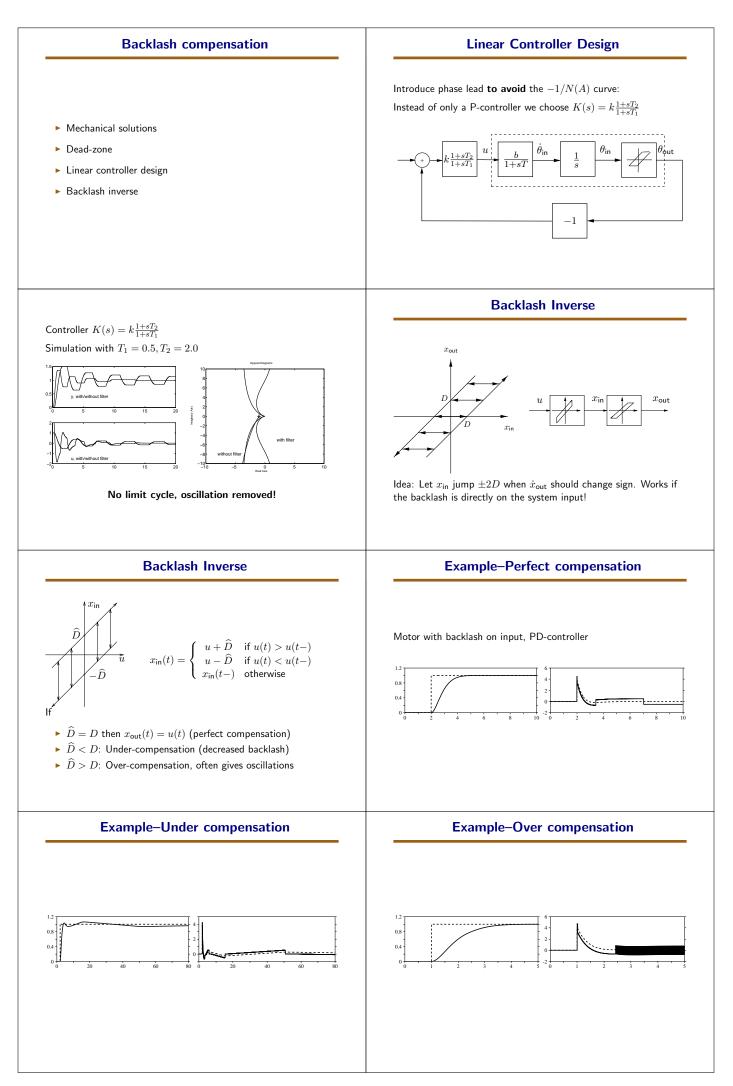
Servo motor with Backlash

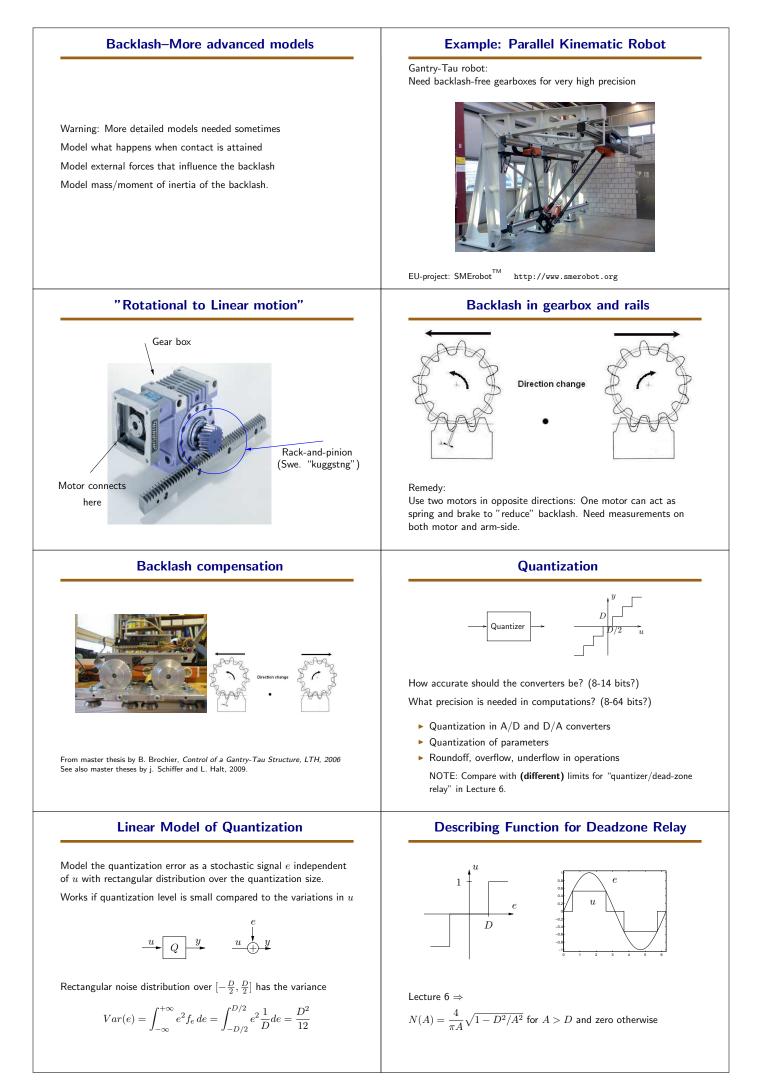
P-control of servo motor



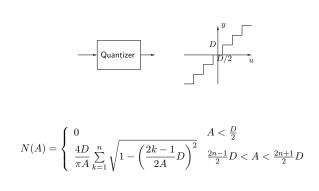
How does the values of K and D affect the behavior?





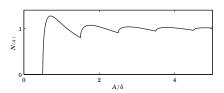






(See exercise)

5 minute exercise



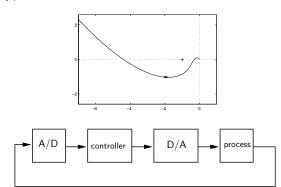
How does the shape of the describing function relate to the number of possible limit cycles and their stability.

What if the Nyquist plot

- \blacktriangleright intersects the negative real axis at -0.80?
- intersects the negative real axis at -1?
- intersects the negative real axis at -2?

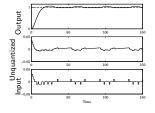
Example – Double integrator with 2nd order controller

Nyquist curve



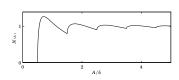
Quantization at D/A converter

Double integrator with 2nd order controller, $D=0.01\,$



Describing function: $A_u \approx D/2 = 0.005$, period T = 39Simulation: $A_u = 0.005$ and T = 39Better prediction, since more sinusoidal signals

Describing Function for Quantizer



The maximum value is $4/\pi \approx 1.27$ for $A \approx 0.71D$.

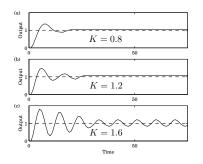
Predicts limit cycle if Nyquist curve intersects negative real axis to the left of $-\pi/4\approx-0.79.$

Should design for gain margin $\not {\it t} \ 1/0.79 {=} \ 1.27!$

Note that reducing ${\cal D}$ only reduces the size of the limit oscillation, the oscillation does not vanish completely.

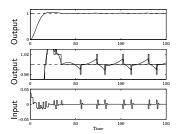
Example – Motor with P-controller.

Roundoff at input, D = 0.2. Nyquist curve intersects at -0.5K. Hence stable for K < 2 without quantization. Stable oscillation predicted for K > 2/1.27 = 1.57.



Quantization at A/D converter

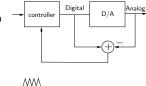
Double integrator with 2nd order controller, $D=0.02\,$



Describing function: $A_y \approx D/2 = 0.01$, period T = 39Simulation: $A_y = 0.01$ and T = 28

Quantization Compensation

- Use improved converters, (small quantization errors/larger word length)
- Linear design, avoid unstable controller, ensure gain margin¿1.3
- Use the tracking idea from anti-windup to improve D/A converter
- Use analog dither, oversampling and digital low-pass filter to improve accuracy of A/D converter



filter

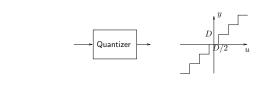
decim

A/D

Today's Goal

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• Be able to analyze the effect of quantization errors



No More Lecture This Week!

Next time on Friday next week: November 25