

Choice of Tracking Time T_t



With very small T_t (large gain $1/T_t$), spurious errors can saturate the output, which leads to accidental reset of the integrator. Too large T_t gives too slow reaction (little effect).

The tracking time T_t is the design parameter of the anti-windup. Common choices: $T_t = T_i$ or $T_t = \sqrt{T_i T_d}$.

Antiwindup – General State-Space Controller

State-space controller:

$$\dot{x}_c(t) = Fx_c(t) + Gy(t) u(t) = Cx_c(t) + Dy(t)$$

Windup possible if F is unstable and u saturates.



Idea:

Rewrite representation of control law from (a) to (b) such that:

(a) and (b) have same input-output relation

(b) behaves better when feedback loop is broken, if S_B stable

State-space controller without and with anti-windup:



Saturation

Optimal control theory (later)

Multi-loop Anti-windup (Cascaded systems):

Difficult problem, several suggested solutions Turn off integrator in outer loop when inner loop saturates

State feedback with Observer



$$\dot{\hat{x}} = A\hat{x} + B\operatorname{sat}(v) + K(y - C\hat{x})$$

 $v = L(x_m - \hat{x})$

 \hat{x} is estimate of process state, x_m desired (model) state. Need model of saturation if $\mathrm{sat}(v)$ is not measurable

Antiwindup – General State-Space Controller

Mimic the observer-based controller:

$$\dot{x}_c = Fx_c + Gy + K \underbrace{(u - Cx_c - Dy)}_{=0}$$
$$= (F - KC)x_c + (G - KD)y + Ku$$
$$= F_0x_c + G_0y + Ku$$

Design so that $F_0 = F - KC$ has desired stable eigenvalues Then use controller

$$\dot{x}_c = F_0 x_c + G_0 y + K u$$

 $u = \operatorname{sat} (C x_c + D y)$

5 Minute Exercise

How would you do antiwindup for the following state-feedback controller with observer and integral action ?



Friction

Present almost everywhere

- Often bad
- Friction in valves and mechanical constructions
- Sometimes good
- Friction in brakes
 Sometimes too small
 - Earthquakes

Problems

- How to model friction
- ▶ How to compensate for friction





